## Strictly Confidential - (For Internal and Restricted Use Only) Secondary School Examination-2020 Marking Scheme - Mathematics 30/1/1, 30/1/2, 30/1/3

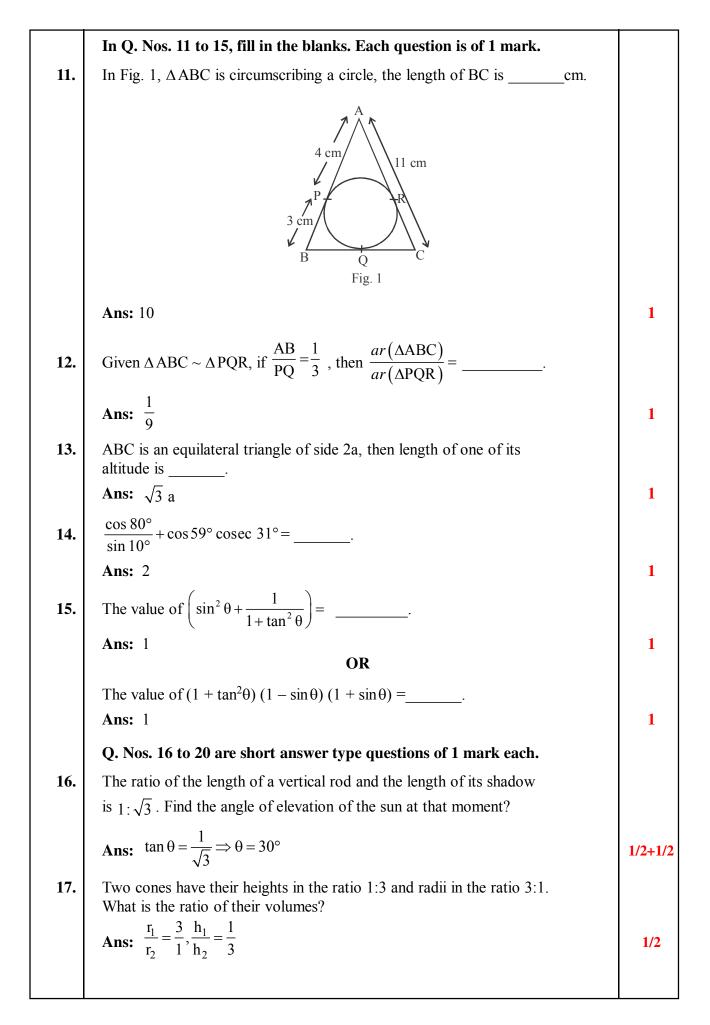
## General instructions

- 1. You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully. **Evaluation is a 10-12 days mission for all of us. Hence, it is necessary that you put in your best efforts in this process.**
- 2. Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one's own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and marks be awarded to them. In class-X, while evaluating two competency based questions, please try to understand given answer and even if reply is not from marking scheme but correct competency is enumerated by the candidate, marks should be awarded.
- **3.** The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
- 4. Evaluators will mark( $\sqrt{}$ ) wherever answer is correct. For wrong answer 'X"be marked. Evaluators will not put right kind of mark while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.
- **5.** If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.
- 6. If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.
- 7. If a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out.
- 8. No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
- 9. A full scale of marks \_\_\_\_\_(example 0-100 marks as given in Question Paper) has to be used. Please do not hesitate to award full marks if the answer deserves it.
- **10.** Every examiner has to necessarily do evaluation work for full working hours i.e. 8 hours every day and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines).
- 11. Ensure that you do not make the following common types of errors committed by the Examiner in the past:-
  - Leaving answer or part thereof unassessed in an answer book.
  - Giving more marks for an answer than assigned to it.
  - Wrong totaling of marks awarded on a reply.
  - Wrong transfer of marks from the inside pages of the answer book to the title page.
  - Wrong question wise totaling on the title page.
  - Wrong totaling of marks of the two columns on the title page.
  - Wrong grand total.
  - Marks in words and figures not tallying.
  - Wrong transfer of marks from the answer book to online award list.
  - Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the X for incorrect answer.)
  - Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
- 12. While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as cross (X) and awarded zero (0)Marks.
- 13. Any unassessed portion, non-carrying over of marks to the title page, or totaling error detected by the candidate shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
- 14. The Examiners should acquaint themselves with the guidelines given in the Guidelines for spot Evaluation before starting the actual evaluation.
- **15.** Every Examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totaled and written in figures and words.
- **16.** The Board permits candidates to obtain photocopy of the Answer Book on request in an RTI application and also separately as a part of the re-evaluation process on payment of the processing charges.

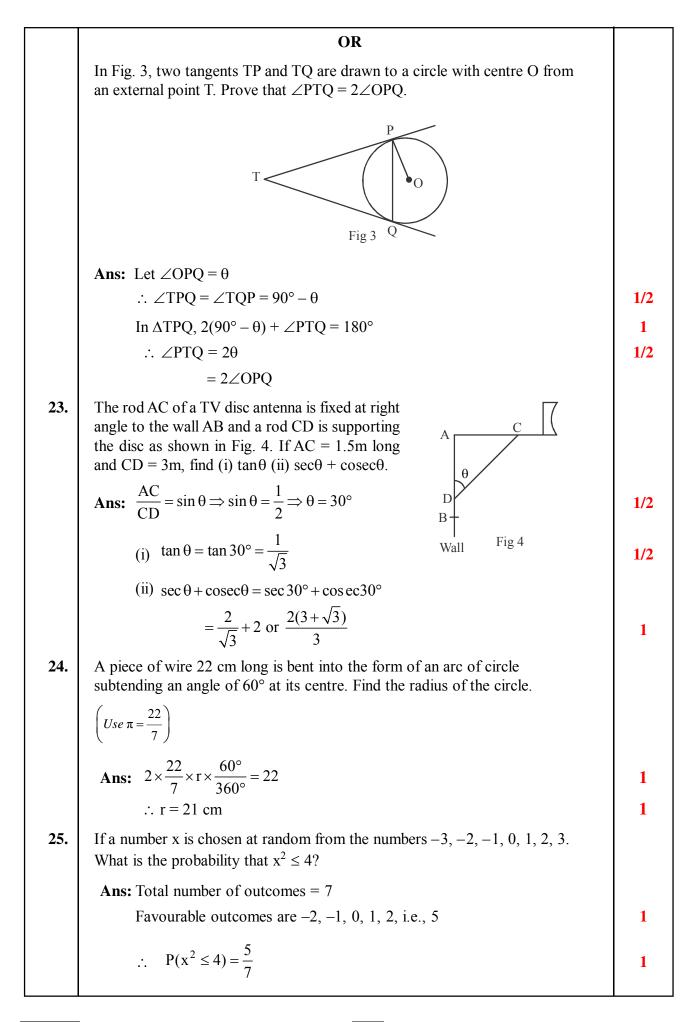
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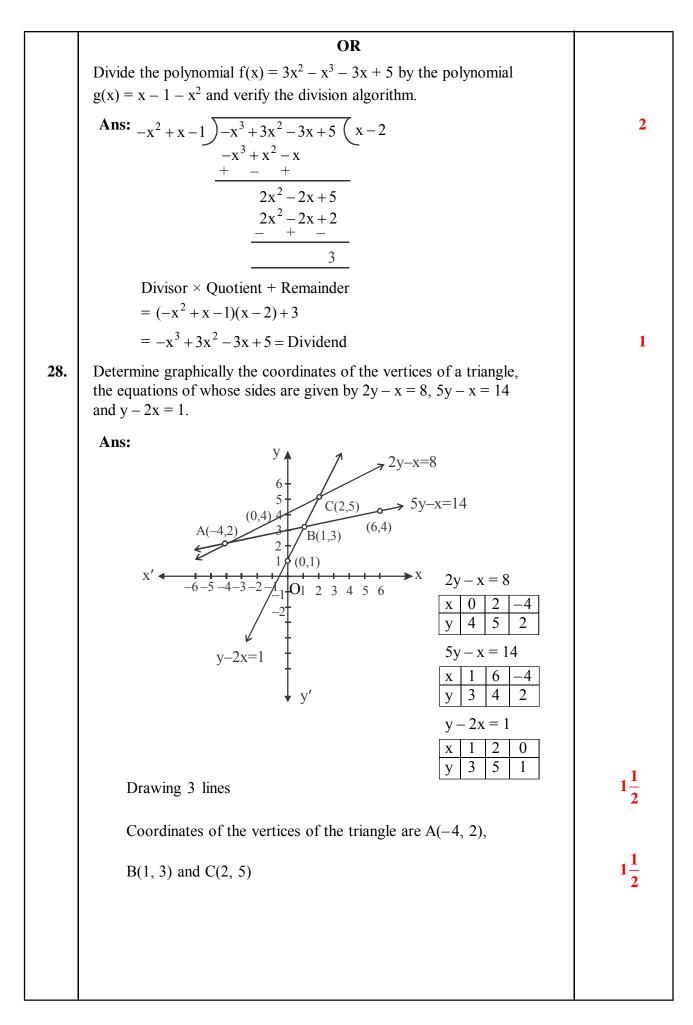
	E	QUESTION PAPH XPECTED ANSWE SECTIO	R/VALUE POINTS	5	
		multiple choice type	e question of 1 mark	each.	
	Select the correct of	option.			Maarlan
Q.No.					Marks
1.	If one of the zeroes of k is	of the quadratic poly	nomial $x^2 + 3x + k$ is	2, then the value	
	<b>(a)</b> 10	<b>(b)</b> −10	( <b>c</b> ) –7	( <b>d</b> ) -2	
	<b>Ans:</b> (b) -10				1
2.	The total number of	f factors of a prime m	umber is		
	<b>(a)</b> 1	<b>(b)</b> 0	(c) 2	( <b>d</b> ) 3	
	<b>Ans:</b> (c) 2				1
3.	The quadratic polyr 6, is	nomial, the sum of wh	ose zeroes is -5 and	their product is	
		<b>(b)</b> $x^2 - 5x + 6$	(c) $x^2 - 5x - 6$	$(\mathbf{d}) - x^2 + 5x + 6$	
	<b>Ans:</b> (a) $x^2 + 5x + $	6			1
4.	The value of k for $x = 3$ has no s	which the system of ecolution, is	quations $x + y - 4 = 0$	0 and	
	( <b>a</b> ) –2	<b>(b)</b> ≠2	(c) 3	( <b>d</b> ) 2	
	<b>Ans:</b> (d) 2				1
5.	The HCF and the L	CM of 12, 21, 15 res	pectively are		
	<b>(a)</b> 3,140	<b>(b)</b> 12,420	( <b>c</b> ) 3,420	( <b>d</b> ) 420,3	
	<b>Ans:</b> (c) 3,420				1
6.		which $2x_{x}(x + 10)$ and	(3x+2) are the thr	ee	
	consecutive terms $c$	of an AP, 1s (b) –6	( <b>c</b> ) 18	( <b>d</b> ) -18	
	(a) $6$	(0) =0	$(\mathbf{C})$ 18	(u) = 10	1
-	Ans: (a) 6	AD is n and the same	non difforence is a t	han ita 10th tarma ia	
7.		AP is p and the commute $(\mathbf{b})$ p $\mathbf{Q}_{\mathbf{c}}$	-		
	(a) q + 9p Ans: (c) p + 9q	( <b>b</b> ) p – 9q	( <b>c</b> ) p + 9q	( <b>d</b> ) 2p + 9q	1
8.		en the naints (a and a	$+ h \sin \theta$ (1) and (0)	$a \sin A_{-} + \cos A_{-}$	
0.		en the points (a $\cos \theta$			
	(a) $a^2 + b^2$	<b>(b)</b> $a^2 - b^2$	(c) $\sqrt{a^2+b^2}$	(d) $\sqrt{a^2-b^2}$	
	<b>Ans:</b> (c) $\sqrt{a^2 + b^2}$				1
9.	If the point P(k, 0)	divides the line segme 0 1 : 2, then the value		A(2, -2) and	
	(a) 1	( <b>b</b> ) 2	(c) -2	( <b>d</b> ) −1	
	<b>Ans:</b> (d) –1	· ·		~ /	1
10.	The value of p, for	which the points A(3,	1), B(5, p) and C(7,	-5) are collinear, is	
	( <b>a</b> ) -2	( <b>b</b> ) 2	(c) -1	( <b>d</b> ) 1	
	<b>Ans:</b> (a) –2				1



18. 19.	$\therefore \text{ Ratio of volumes} = \frac{\frac{1}{3}\pi r_1^2 h_1}{\frac{1}{3}\pi r_2^2 h_2} = 3:1$ A letter of English alphabet is chosen at random. What is the probability that the chosen letter is a consonant. <b>Ans:</b> P (consonant) = $\frac{21}{26}$ A die is thrown once. What is the probability of getting a number less than 3? <b>Ans:</b> P (number less than 3) = $\frac{2}{6}$ or $\frac{1}{3}$ <b>OR</b>	1/2 1 1
	If the probability of winning a game is $0.07$ , what is the probability of losing it?	
	If the probability of winning a game is 0.07, what is the probability of losing it?	
	<b>Ans:</b> $P(losing) = 1 - 0.07$	1/2
	= 0.93	1/2
20.	If the mean of first n natural number is 15, then find n.	
	n(n+1)	
		1.10
	<b>Ans:</b> $\frac{2}{n} = 15$	1/2
	$\therefore$ n = 29	1/2
		1/2
	SECTION – B	
	Q. Nos. 21 to 26 carry 2 marks each.	
21.	Show that $(a - b)^2$ , $(a^2 + b^2)$ and $(a + b)^2$ are in AP.	
21.		
	<b>Ans:</b> $(a^2 + b^2) - (a - b)^2 = 2ab$	1
	$(a+b)^2 - (a^2 + b^2) = 2ab$	1
	Common difference is same. ∴ given terms are in AP	
22.	In Fig. 2 DE   AC and DC   AP. Prove that $\frac{BE}{EC} = \frac{BC}{CP}$ .	
	EC CP	
	B E C P Fig 2	
	<b>Ans:</b> In $\triangle ABC$ , DE    AC, $\therefore \frac{BD}{DA} = \frac{BE}{EC}$ (i)	1
	In $\triangle ABP$ , DC    AP, $\therefore \frac{BD}{DA} = \frac{BC}{CP}$ (ii)	1/2
	From (i) & (ii), $\frac{BE}{EC} = \frac{BC}{CP}$	1/2



26.	Find the	mean	of the	followi	ng distril	oution:					
	Class:		3-5	5-7	7-9	9-11	11-13				
	Frequen	cy:	5	10	10	7	8				
	Ans:	Clas	ses	X <sub>i</sub>	$\mathbf{f}_{i}$	<b>f</b> <sub>x</sub> <b>x</b> <sub>i</sub>					11/2
		3 -	5	4	5	20	1				
		5 –	7	6	10	60					
		7 –	9	8	10	80					
		9 – 1	11	10	7	70					
		11 –	13	12	8	96					
		Tota	al		40	326	1				
			I_	I							
		$\overline{\mathbf{x}} = $	$\sum f_i x_i$	$=\frac{326}{40}$	= 8 15						1/0
		$\Lambda = 1$	$\sum f_i$	40	- 0.15	<b>. .</b>					1/2
	Find the	mada	oftho	fallowin	aa data.	OR					
	Find the Class:	mode	0-20	-	40-60	60-80	80-100	110-120	120-140		
	Frequen	cy:	6	8	10	12	6	5	3		
	Ans: 1	Modal	class : (	50 — 80						1	1/2
			Ø	$f_1 - f_0$	$\overline{\mathbf{f}_2} \times \mathbf{h} =$	60 - 1	2-10	× 20			
	1				$f_2 \wedge f_2$	$\frac{00+}{24}$	-10-6	~ 20			1
		=	60 + 3	5 = 65			~				1/2
	Quastia		have 2	7 to 21		ΓΙΟΝ - mamba					
27.	-				carry 3			ma and a fith			
21.		-	-	•	+ bx $+$ c,		-	orocal of th	le zeroes		
	Ans:	f(x) = a	$ax^2 + b$	x + c							
		$\alpha + \beta =$	$-\frac{b}{c}$ , o	$\alpha\beta = \frac{c}{c}$							1/2
			a	a	1 1	b					
	1	New su	m of z	eroes =	$\frac{1}{\alpha} + \frac{1}{\beta} =$	$-\frac{c}{c}$					1
	1	New pr	oduct o	ofzeroe	$s = \frac{1}{\alpha} \times \frac{1}{\alpha}$	$\frac{1}{\beta} = \frac{a}{c}$					1
	∴ Req	uired q	uardra	tic poly	nomial =	$= x^2 + \frac{1}{\alpha}$	$\frac{2}{c}x + \frac{a}{c}c$	or $\left(cx^2+b\right)$	bx + a		1/2



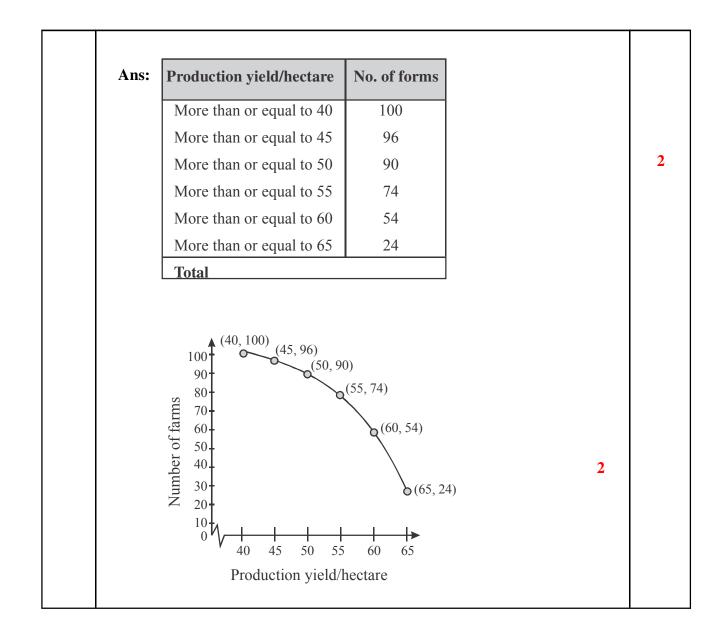
		i
	<b>OR</b> If 4 is the zero of the cubic polynomial $x^3 - 3x^2 - 10x + 24$ , find its other two zeroes.	
	<b>Ans:</b> $x - 4$ is a factor of given polynomial.	
	$\begin{array}{c} x-4  \int x^{3} - 3x^{2} - 10x + 24 \left(x^{2} + x - 6\right) \\ \xrightarrow{x^{3} - 4x^{2}} \\ \xrightarrow{y^{2} - 4x^{2}} \\ \xrightarrow{x^{2} - 4x} \\ \xrightarrow{-/ + } \\ \hline \\ -6x + 24 \\ \xrightarrow{-/ + } \\ \hline \\ 0 \end{array}$	2
	$x^{2} + x - 6 = (x + 3)(x - 2)$	
29.	<ul> <li>∴ Other than zeroes are -3 and 2.</li> <li>In a flight of 600 km, an aircraft was slowed due to bad weather.</li> <li>Its average speed for the trip was reduced to 200 km/hr and time of flight increased by 30 minutes. Find the original duration of flight.</li> </ul>	1
	<b>Ans:</b> Let the speed of aircraft be x km/hr	
	-	
	$\therefore \frac{600}{x - 200} - \frac{600}{x} = \frac{30}{60}$	1
	$\Rightarrow x^2 - 200x - 240000 = 0$	1
	(x - 600) (x + 400) = 0 x = 600, -400 (Rejected) Speed of aircraft = 600 km/hr	1/2
	$\therefore$ Duration of flight = 1 hr	1/2
30.	Find the area of triangle PQR formed by the points $P(-5, 7)$ , $Q(-4, -5)$ and $R(4, 5)$ .	
	Ans: $ar(PQR) = \frac{1}{2} \left[ -5(-5-5) - 4(5-7) + 4(7+5) \right] sq.$ units	2
	$=\frac{1}{2}[50+8+48]$ sq. units	
	= 53 sq. units	1
	OR	
	If the point $C(-1, 2)$ divides internally the line segment joining A(2, 5) and B(x, y) in the ratio 3 : 4, find the coordinates of B.	
	Ans: Coordinates of C arc $\left(\frac{3x+8}{7}, \frac{3y+20}{7}\right) = (-1, 2)$ $\Rightarrow x = -5, y = -2$ $\therefore$ Coordinates of B are $(-5, -2)$ A $(2, 5)$ (-1, 2) (x, y)	$1\frac{1}{2}$
	$\Rightarrow x = -5, y = -2 \qquad \qquad A \xrightarrow{3:4} B$	1
	:. Coordinates of B are $(-5, -2)$ (2, 5) (-1, 2) (x, y)	1/2

31.	In Fig.5, $\angle D = \angle E$ and $\frac{AD}{DB} = \frac{AE}{EC}$ ,	
51.		
	prove that BAC is an isosceles triangle. $D \swarrow E$	
	Ans: $\angle D = \angle E \Rightarrow AE = AD$ $B \angle Fig 5$ C	1
	$\therefore \frac{AD}{DB} = \frac{AE}{EC} \implies DB = EC$	1/2
	$\Rightarrow AD + DB = AE + EC$	1
	$\therefore AB = AC$	1/2
	Hence $\triangle BAC$ is an isosceles triangle.	
32.	In a triangle, if square of one side is equal to the sum of the squares of the other two sides, then prove that the angle opposite to the first side is a right angle.	
	<b>Ans:</b> For correct given, To prove, construction and figure.	$1\frac{1}{2}$ $1\frac{1}{2}$
	For correct proof.	$1\frac{1}{2}$
33.	If $\sin\theta + \cos\theta = \sqrt{3}$ , then prove that $\tan\theta + \cot\theta = 1$ .	
	<b>Ans:</b> $\sin \theta + \cos \theta = \sqrt{3} \implies (\sin \theta + \cos \theta)^2 = (\sqrt{3})^2$	1
	$\sin^2\theta + \cos^2\theta + 2\sin\theta\cos\theta = 3 \Rightarrow \sin\theta\cos\theta = 1$	1
	L.H.S = $\tan \theta + \cot \theta = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = \frac{1}{\cos \theta \sin \theta} = 1 = \text{R.H.S}$	1
34.	A cone of base radius 4 cm is divided into two parts by drawing a plane through the mid-point of its height and parallel to its base. Compare the volume of the two parts.	
	Ans: $\triangle ABC \sim \triangle ADE, \ \frac{h}{2h} = \frac{BC}{4}$	cor. fig 1/2
	$ A \qquad 2h \qquad 4 \qquad $	1
	Ratio of volumes of two parts	
	$= \frac{\frac{1}{3}\pi \times 2^{2} \times h}{\frac{1}{3}\pi \times (2^{2} + 4^{2} + 2 \times 4) \times h}$	
	$ = \frac{1}{\frac{1}{\pi \times (2^2 + 4^2 + 2 \times 4) \times h}} $	1
	$=\frac{4}{28}=\frac{1}{7}$ or 1 : 7 (accept 7 : 1 also)	1/2

.30/1/1.

	SECTION – D	
	Question numbers 35 to 40 carry 4 marks each.	
35.	Show that the square of any positive integer cannot be of form $(5q + 2)$ or $(5q + 3)$ for any integer q.	
	<b>Ans:</b> Let a be any positive integer. Take $b = 5$ as the divisor.	
	$\therefore$ a = 5m + r, r = 0,1,2,3,4	1
	Case-1 : $a = 5m \Rightarrow a^2 = 25m^2 = 5(5m^2) = 5q$	1/2
	Case-2 : $a = 5m+1 \implies a^2 = 5(5m^2 + 2m) + 1 = 5q + 1$	for
	Case-3 : $a = 5m+2 \implies a^2 = 5(5m^2 + 4m) + 4 = 5q + 4$	each
	Case-4 : $a = 5m+3 \implies a^2 = 5(5m^2 + 6m + 1) + 4 = 5q + 4$	case
	Case-5 : $a = 5m+4 \implies a^2 = 5(5m^2 + 8m + 3) + 1 = 5q + 1$	$=2\frac{1}{2}$
	Hence square of any positive integer cannot be of the form $(5q + 2)$ or $(5q + 3)$ for any integer q.	1/2
	OR	
	Prove that one of every three consecutive positive integers is divisible by 3. Ans: Let n be any positive integer. Divide it by 3.	
	$\therefore$ n = 3q + r, r = 0, 1, 2	1
	Case-1 : $n = 3q$ (divisible by 3)	
	n + 1 = 3q + 1, n + 2 = 3q + 2	1 for
	Case-2 : $n = 3q + 1 \Rightarrow n + 1 = 3q + 2$ , $n + 2 = 3q + 3$ (divisible by 3)	each
	Case-3 : $n = 3q + 2 \implies n + 1 = 3q + 3$ (divisible by 3), $n + 2 = 3q + 4$	case = 3
36.	The sum of four consecutive numbers in AP is 32 and the ratio of product of the first and last terms to the product of two middle terms is 7:15. Find the numbers.	
	Ans: Let four consecutive number be $a - 3d$ , $a - d$ , $a + d$ , $a + 3d$	1/2
	Sum = 32 $\therefore$ 4a = 32 $\Rightarrow$ a = 8	1/2
	$\frac{(a-3d)(a+3d)}{(a-d)(a+d)} = \frac{7}{15} \Longrightarrow 15(64-9d^2) = 7(64-d^2)$	1
	$\therefore d^2 = 4 \implies d = \pm 2$	1
	Four numbers are 2, 6, 10, 14.	1
	OR	
	Solve: $1+4+7+10++x=287$	
	<b>Ans:</b> $x = a_n = 1 + 3n - 3 = 3n - 2$	1
	$S_n = 287 \Longrightarrow \frac{n}{2} [1 + 3n - 2] = 287$	1
	$\therefore  3n^2 - n - 574 = 0$	1/2
	$(n-14)(3n+41) = 0 \Longrightarrow n = 14$	1
	$\therefore x = 3n - 2 = 40$	1/2

37.	Draw a line segment AB of length 7 cm. Taking A as centre, draw a circle of radius 3 cm and taking B as centre, draw another circle of radius 2 cm. Construct tangents to each circle from the centre of the other circle.	
	<b>Ans:</b> Constructing the circles of radii 3 cm and 2 cm. Constructing the tangents.	1 3
38.	A vertical tower stands on a horizontal plane and is surmounted by a vertical flag-staff of height 6 m. At a point on the plane, the angle of elevation of the bottom and top of the flag-staff are 30° and 45° re-	
	spectively. Find the height of the tower. (Take $\sqrt{3} = 1.73$ )	
	Ans:	cor. fig 1
	$\frac{h}{x} = \tan 30^{\circ}$ $\Rightarrow x = h\sqrt{3}$	1
	$\frac{6+h}{x} = \tan 45^\circ \implies 6+h = x$	1
	h $\therefore h = \frac{6}{\sqrt{3}-1} = 3(\sqrt{3}+1) = 3 \times 2.73 \text{ m}$ = 8.19  m	1
	$C \xrightarrow{X} D = 8.19 \text{ m}$	
39.	A bucket in the form of a frustum of a cone of height 30 cm with radii of its lower and upper ends as 10 cm and 20 cm respectively. Find the capacity of the bucket. Also find the total cost of milk that can completely fill the	
	bucket at the rate of 40 per litre. $\left( \text{Use } \pi = \frac{22}{7} \right)$	
	<b>Ans:</b> Capacity of bucket = $\frac{1}{3}\pi h \left( r_1^2 + r_2^2 + r_1 r_2 \right)$	
	$= \frac{1}{3} \times \frac{22}{7} \times 30 \left( 10^2 + 20^2 + 10 \times 20 \right) \text{cm}^3$	1
	$= 22000 \text{ cm}^3$	$1\frac{1}{2}$
	= 221	1/2
	$Cost of milk = 40 \times 22 = 880$	1
40.	The following table gives production yield per hectare (in quintals) of wheat of 100 farms of a village:	
	Production yield/hect. 40-45 45-50 50-55 55-60 60-65 65-70	
	No. of farms         4         6         16         20         30         24	
	Change the distribution to 'a more than' type distribution and draw its ogive.	



The median if total frequ			-	data i	0 s 525		the v	alues of	x and	у,		
Class :	0-100	100-200	200-300	300-400	400-500	500-600	600-700	700-800	800-900	900-1000		
Frequency:	2	5	х	12	17	20	у	9	7	4		
Ans:											1	
Classe	es		Frequ	iency		nulativo uency	è					
0-100			2		псч	2						
100-200			5			7						
200-300			x		7	+ x						
300-400			12	2	19	$\mathbf{y} + \mathbf{x}$						
400-500			17	7	30	5 + x						
500-600			20	)	50	5 + x		→ Med	ian clas	S		2
600-700			у		56 -	+x + y						
700-800			9			+ x+ y						
800-900			7			+ x+ y						
900-1000			4		76 -	+ x+ y						
Total			10	0								
76 + x - 500 - 6 Median $\Rightarrow 525$	500 is $n = \ell$	the frequencies the n $+\frac{\frac{n}{2}}{f}$	median cf —×h	n class	3							1/
Solving			= 9									1
From (	i), y =	= 15										1/2